

Name: Key

Geometry

Date: _____ Per: _____

Unit 10: Circles

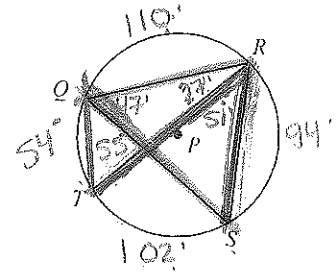
Classwork

Inscribed Angles, Tangents, Angle & Arc Measures

Inscribed Angles

1-5 1. In circle P, if $m\widehat{QR} = 110^\circ$, $m\widehat{RS} = 94^\circ$, and $m\angle QRT = 27^\circ$, find each measure.

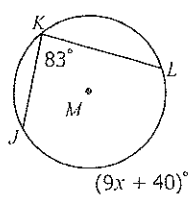
- a) $m\angle QTR = 55^\circ$
- b) $m\angle RQS = 47^\circ$
- c) $m\widehat{TS} = 102^\circ$
- d) $m\angle TRS = 51^\circ$
- e) $m\angle QSR = 55^\circ$
- f) $m\widehat{QT} = 54^\circ$



For questions 2-5, find each value or measure.

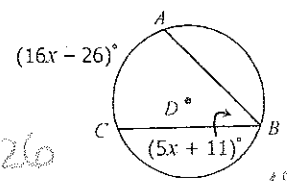
2. $x = 14$

* 2 angle = arc
 $2(83) = 9x + 40$
 $166 = 9x + 40$
 -40
 $126 = 9x$
 $\frac{126}{9} = \frac{9x}{9}$
 $x = 14$



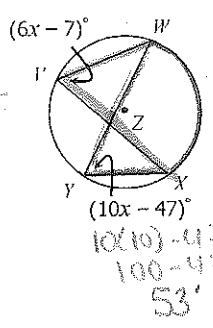
3. $m\angle ABC = 51^\circ$

* 2 angle = arc
 $2(5x + 11) = 16x - 26$
 $10x + 22 = 16x - 26$
 $-10x$
 $22 = 6x - 26$
 $+26$
 $48 = 6x$
 $\frac{48}{6} = \frac{6x}{6}$
 $x = 8$



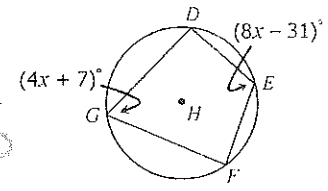
4. $m\widehat{WX} = 106^\circ$

* 2 chords cutting same arc so they are congruent.
 $6x - 7 = 10x - 47$
 $-6x$
 $-7 = 4x - 47$
 $+47$
 $40 = 4x$
 $\frac{40}{4} = \frac{4x}{4}$
 $x = 10$
Tangents: 6-10

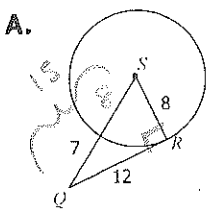


5. $m\angle DGF = 75^\circ$

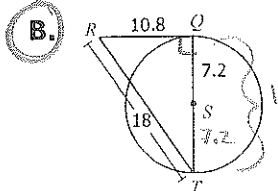
* opposite angles supp.
 $4x + 7 + 8x - 31 = 180$
 $12x - 24 = 180$
 $+24$
 $12x = 204$
 $\frac{12x}{12} = \frac{204}{12}$
 $x = 17$



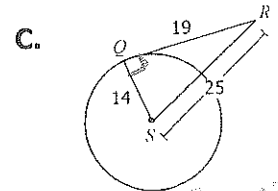
6. In which of the following diagrams is \overline{QR} tangent to circle S? Circle the best answer.



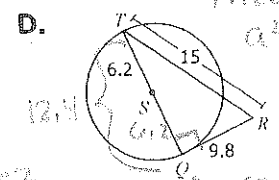
$8^2 + 12^2 = 15^2$
 $64 + 144 = 225$
 $208 \neq 225$
 NO



$(10, 8)^2 + (14, 4)^2 = 18^2$
 $116.64 + 207.36 = 324$
 $324 = 324$
 YES



$14^2 + 19^2 = 25^2$
 $196 + 361 = 625$
 $557 \neq 625$
 NO



* use Pythagorean theorem
 $a^2 + b^2 = c^2$
 $(12, 4)^2 + (9, 8)^2 = 15^2$
 $153.76 + 96.04 = 225$
 $249.8 \neq 225$
 NO

For questions 7-10, find each value or measure. Assume that segments that appear to be tangent are tangent.

7. $AC = \underline{23.3}$

$$a^2 + b^2 = c^2$$

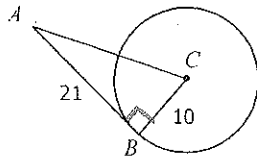
$$10^2 + 21^2 = c^2$$

$$100 + 441 = c^2$$

$$541 = c^2$$

$$\sqrt{541} = \sqrt{c^2}$$

$$23.3 = c$$



8. $ML = \frac{1}{2}(12.8) = \underline{6.4}$

$$a^2 + b^2 = c^2$$

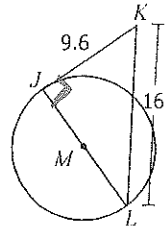
$$(9.6)^2 + b^2 = 16^2$$

$$92.16 + b^2 = 256$$

$$-92.16 \quad -92.16$$

$$b^2 = 163.84$$

$$\sqrt{b^2} = \sqrt{163.84}$$



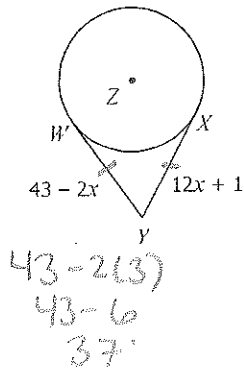
9. $WY = \underline{37}$

$$43 - 2x = 12x + 1$$

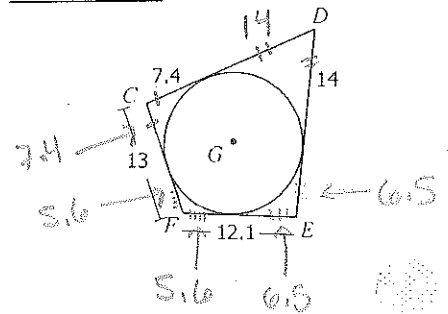
$$\frac{+2x \quad +2x}{43 = 14x + 1}$$

$$\frac{-1 \quad -1}{42 = 14x}$$

$$\frac{14 \quad 14}{3 = x}$$



10. Perimeter of CDEF = 67



Arcs and Angle Measure: 11-20

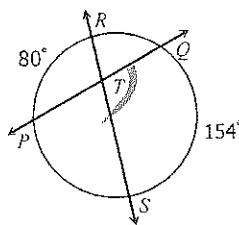
For questions 11-20, find each value or measure.

11. $m\angle QTS = \underline{117^\circ}$

property: 1

Vertical Arcs = $\frac{1}{2}$

$$\frac{154 + 80}{2} = \frac{1}{2}$$



12. $m\widehat{JH} = \underline{34^\circ}$

property: 1

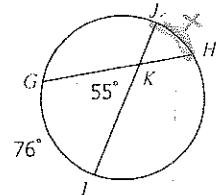
Vertical arcs = $\frac{1}{2}$

$$\frac{76 + x}{2} = 55$$

$$76 + x = 110$$

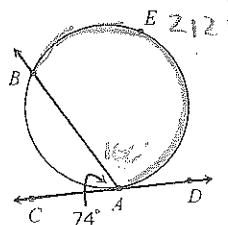
$$-76 \quad -76$$

$$x = 34$$



13. $m\widehat{BEA} = \underline{212^\circ}$

property: 2



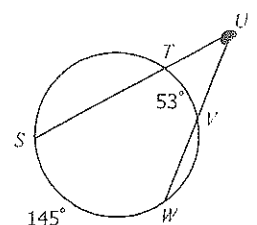
14. $m\angle TUV = \underline{46^\circ}$

property: 3

Big-Little = $\frac{1}{2}$

$$\frac{145 - 53}{2} = \frac{1}{2}$$

$$46 = \frac{1}{2}$$



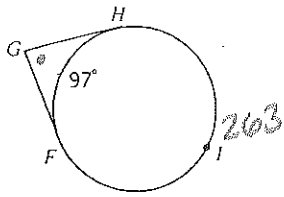
15. $m\angle FGH = 83^\circ$

property: 3

$\frac{B16-L111e}{2} = 4$

$\frac{263-97}{2} = 4$

$83 = 4$



16. $m\widehat{PM} = 139^\circ$

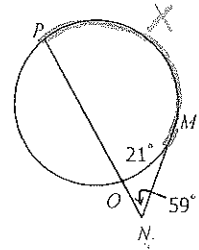
property: 3

$\frac{B16-L111e}{2} = 4$

$\frac{X-21}{2} = 59$

$X-21 = 118$
 $+21 \quad +21$

$X = 139$



17. $x = 16$

property: 1

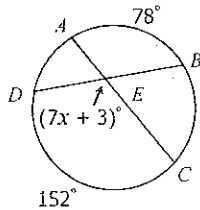
$\frac{\text{Vertical arcs}}{2} = 4$

$\frac{152+78}{2} = 7x+3$

$115 = 7x+3$
 $-3 \quad -3$

$\frac{112-7x}{7} = \frac{7x}{7}$

$x = 16$



18. $x = 5$

property: 2

$2\text{angle} = \text{arc}$

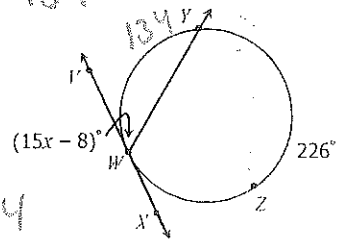
$2(15x-8) = 134$

$30x-16 = 134$

$+16 \quad +16$

$\frac{30x = 150}{30 \quad 30}$

$x = 5$



19. If $m\widehat{ML} = (11x-5)^\circ$, $m\widehat{JK} = (4x+26)^\circ$ and $m\angle MNL = (10x-12)^\circ$, find $m\angle MNL$.

$\frac{\text{Vertical Arcs}}{2} = 4$

$\frac{11x-5 + 4x+26}{2} = 10x-12$

$\frac{15x+21}{2} = 10x-12$

19. $m\angle MNL = \frac{10(9)-12}{90-12} = 78$

property: 1

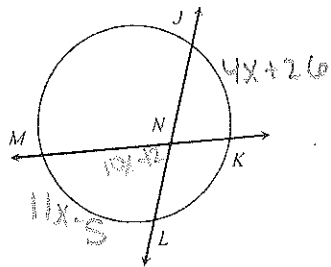
$2(10x-12) = 15x+21$
 $20x-24 = 15x+21$
 $-15x \quad -15x$

$5x-24 = 21$

$+24 \quad +24$

$\frac{5x = 45}{5 \quad 5}$

$x = 9$



20. If $m\widehat{SW} = (12x-5)^\circ$, $m\widehat{TV} = (2x+7)^\circ$, and $m\angle TUV = (6x-19)^\circ$, find $m\widehat{SW}$.

$\frac{B16-L111e}{2} = 4$

$\frac{12x-5 - (2x+7)}{2} = 6x-19$

$\frac{10x-12}{2} = 6x-19$

20. $m\widehat{SW} = \frac{12(13)-5}{151} = 151$

property: 3

$10x-12 = 2(6x-19)$
 $10x-12 = 12x-38$
 $-10x \quad -10x$

$-12 = 2x-38$

$+38 \quad +38$

$\frac{26 = 2x}{2 \quad 2} \quad x = 13$

