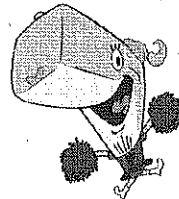


Name: _____

Date: _____



5.6 & 5.7 Practice Problems

**Directions:** Use long division to divide.

1. $(-40x - 8x^3 + 19x^2 + 22 + 3x^4) \div (-2 + 3x)$

$$\begin{array}{r}
 \overline{) 3x^4 - 8x^3 + 19x^2 - 40x + 22} \\
 \underline{-3x^4 + 2x^3} \\
 -6x^3 + 19x^2 - 40x + 22 \\
 \underline{+6x^3 - 4x^2} \\
 15x^2 - 40x + 22 \\
 \underline{-15x^2 + 10x} \\
 -30x + 22 \\
 \underline{+36x - 70} \\
 2
 \end{array}$$

2. $(9n^5 - 6n^4 - 90n + 64) \div (9n - 6)$

$$\begin{array}{r}
 \overline{) 9n^5 - 6n^4 + 0n^3 + 0n^2 - 90n + 64} \\
 \underline{-9n^5 + 6n^4} \\
 -90n + 64 \\
 \underline{+90n - 60} \\
 4
 \end{array}$$

Directions: (A) Evaluate the given function at the given value
 (B) What is the divisor?
 (C) Is it a factor?

3. $f(a) = 3a^4 - 21a^3 + 30a^2 + 11$ at $a = -5$

(A) 5261

(B) $(x+5)$

(C) NO

4. $f(a) = -6a^6 + 32a^5 - 5a^4 - 30a^3 + 19a^2 + 35a - 25$ at $a = 5$

(A) 0

(B) $(x-5)$

(C) yes

Directions: Use the Rational Root Theorem to find all zeros.

5. $x^4 - 2x^3 + x^2 - 8x - 12 = 0$

Possible Roots: $\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12$

$$\frac{p}{q} = \frac{\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12}{\pm 1}$$

Actual Roots: $-1, 3, 2i, -2i$

Factored Form: $(x-3)(x^2+4)(x+1)$

$$\begin{array}{r} 1 \mid 1 \quad -2 \quad 1 \quad -8 \quad -12 \\ \quad \downarrow \quad 1 \quad -1 \quad 0 \quad -8 \\ \hline 1 \quad -1 \quad 0 \quad -8 \quad \underline{-20} \end{array}$$

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$$\begin{array}{r} -1 \mid 1 \quad -2 \quad 1 \quad -8 \quad -12 \\ \quad \downarrow \quad -1 \quad 3 \quad -4 \quad 12 \\ \hline 1 \quad -3 \quad 4 \quad -12 \quad \underline{0} \end{array}$$

$$\begin{aligned} &x^3 - 3x^2 + 4x - 12 \\ &x^2(x-3) + 4(x-3) \\ &(x-3)(x^2+4) = 0 \end{aligned}$$

6. $2x^4 + x^3 - 16x^2 - 5x + 30 = 0$

Possible Roots:

$\pm 1, \pm 2, \pm 3, \pm 5, \pm 6, \pm 10, \pm 15, \pm 30, \pm 1/2, \pm 3/2, \pm 5/2$

$$\frac{p}{q} = \frac{\pm 1, \pm 2, \pm 3, \pm 5, \pm 6, \pm 10, \pm 15, \pm 30}{\pm 1, \pm 2}$$

Actual Roots:

$\pm 15/2, -2, \sqrt{5}, -\sqrt{5}, 3/2$

Factored Form:

$(2x-3)(x^2-5)(x+2)$

$$\begin{array}{r} -2 \mid 2 \quad 1 \quad -16 \quad -5 \quad 30 \\ \quad \quad -4 \quad 6 \quad 20 \quad -30 \\ \hline 2 \quad -3 \quad -10 \quad 15 \quad \underline{0} \end{array}$$

$$2x^3 - 3x^2 - 10x + 15$$

$$x^2(2x-3) - 5(2x-3)$$

$$(2x-3)(x^2-5)$$