

Remainder Theorem & Rational Root Theorem

JEOPARDY

100 POINTS:

$$2(3)^5 - 3(3)^2 - 17(3) + 1$$

Given: $f(x) = 2x^5 - 3x^2 - 17x + 1$

- (a) Is $x - 3$ a factor? NO, when you plug $x=3$ in you get 409.
- (b) Why or why not? remainder not 0

200 POINTS:

$$(-5)^4 + 9(-5)^3 + 23(-5)^2 + 21(-5) + 30$$

Given: $f(x) = x^4 + 9x^3 + 23x^2 + 21x + 30$

- (a) Is -5 a solution? yes, because remainder 0.
- (b) If yes, what is the factor? $(x+5)$

300 POINTS:

Factor: $18y^4 - 15y^3 + 3y^2$

$$3y^2(6y^2 - 5y + 1)$$

$$\boxed{3y^2(3y-1)(2y-1)} \text{ Answer}$$

400 POINTS:

Use the Rational Root Theorem to find all roots.

$$f(x) = x^4 + x^3 + 7x^2 + 9x - 18$$

(You can use back of this paper for work!)

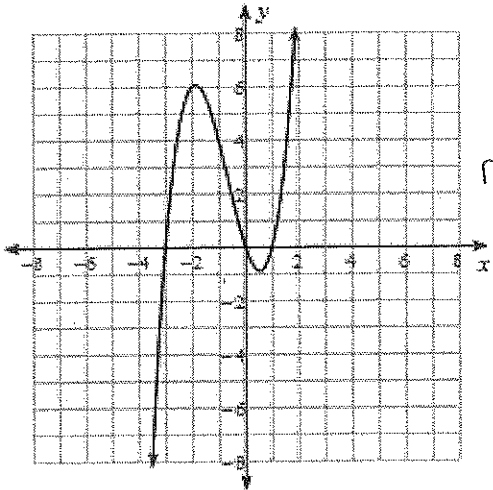
Possible Roots: $\pm 1 \pm 2 \pm 3 \pm 6 \pm 9 \pm 18$

Actual Roots: $3i, -3i, -2, 1$

Factored Form: $(x^2 + 9)(x+2)(x-1)$

JEOPARDY

Writing

100 POINTS:

roots:
-3, 0, 1

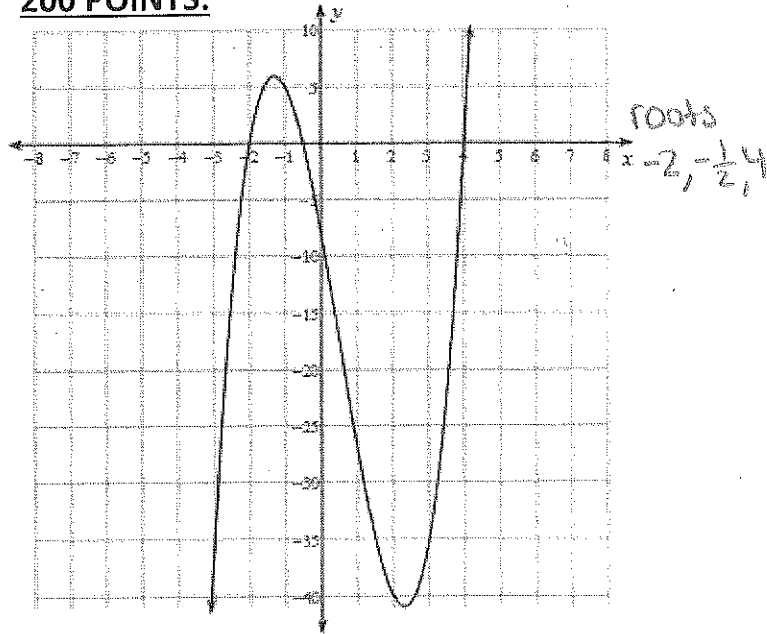
$$x(x-1)(x+3)$$

$$(x^2 - x)(x+3)$$

$$x^3 + 3x^2 - x^2 - 3x$$

$$x^3 + 2x^2 - 3x$$

Answer

200 POINTS:

roots
-2, -1/2, 4

$$(x+2)(2x+1)(x-4)$$

$$(2x^2 + 5x + 2)(x-4)$$

$$2x^3 - 8x^2 + 5x^2 - 20x + 2x - 8$$

$$2x^3 - 3x^2 - 18x - 8$$

300 POINTS:

Write the equation of the polynomial with roots:

-1 multiplicity 2 and 3i

$$(x+1)(x+1)(x^2+9)$$

$$(x^2+2x+1)(x^2+9)$$

$$x^4 + 9x^2 + 2x^3 + 18x + x^2 + 9$$

$$x^4 + 2x^3 + 10x^2 + 18x + 9$$

400 POINTS:

Write the equation of the polynomial with roots:

$-\frac{5}{2}$ and $\sqrt{6}$

$$(2x+5)(x^2-6)$$

$$2x^3 - 12x + 5x^2 - 30$$

$$2x^3 + 5x^2 - 12x - 30$$

JEOPARDY

Multiplying & Dividing

100 POINTS:

What is the difference between synthetic division and long division?
You can only use synthetic division when you have a leading coefficient of 1 and degree 1 for the divisor.

200 POINTS:

Multiply. $(3x - 2)(x^3 - 6x + 1)$

$$3x^4 - 18x^2 + 3x - 2x^3 + 12x - 2$$
$$\boxed{3x^4 - 2x^3 - 18x^2 + 15x - 2} \text{ Answer}$$

300 POINTS:

Multiply. $(3x^2y^5 - 11x)(-4x^3 - 3y^2 + 7)$

$$-12x^5y^5 - 9x^2y^7 + 21x^2y^5 + 44x^4 + 33xy^2 - 77x$$

$$\boxed{-12x^5y^5 + 44x^4 - 9x^2y^7 + 21x^2y^5 + 33xy^2 - 77x}$$

400 POINTS:

Use Synthetic Division. $(x^3 - 28x - 48) \div (x + 4)$

$$\begin{array}{r|rrrr} -4 & 1 & 0 & -28 & -48 \\ & \downarrow & -4 & 16 & 48 \\ \hline & 1 & -4 & -12 & 0 \end{array}$$

$$\boxed{x^2 - 4x - 12}$$

500 POINTS:

Use long division. $(-70v - 38v^3 + 57 + 28v^4 - 56v^2 + 16v^5) \div (10 + 4v)$

$$\begin{array}{r} \boxed{4v^4 - 3v^3 - 2v^2 - 9v + 57} \leftarrow \text{Answer} \\ 4v + 10 \overline{) 16v^5 + 28v^4 - 38v^3 - 56v^2 - 70v + 57} \\ \underline{-16v^5 + 40v^4} \\ -12v^4 - 38v^3 - 56v^2 - 70v + 57 \\ \underline{+12v^4 + 30v^3} \\ -8v^3 - 56v^2 - 70v + 57 \\ \underline{+8v^3 + 20v^2} \\ -36v^2 - 70v + 57 \\ \underline{+36v^2 + 90v} \\ 20v + 57 \\ \underline{-20v - 50} \\ 7 \end{array}$$

JEOPARDY

Factor & Solve

100 POINTS:

Solve.

$$(3x^3 - 2x^2)(-9x + 6) = 0$$

$$x^2(3x-2) - 3(3x-2) = 0$$

$$(x^2-3)(3x-2) = 0$$

$$\left. \begin{array}{l} x^2-3=0 \\ x^2=3 \\ x=\pm\sqrt{3} \end{array} \right\} \begin{array}{l} 3x-2=0 \\ x=2/3 \end{array}$$

Roots: $\sqrt{3}, -\sqrt{3}, \frac{2}{3}$

200 POINTS:

Solve.

$$x^4 - 13x^2 + 36 = 0$$

$$(x^2-9)(x^2-4) = 0$$

$$\left. \begin{array}{l} x^2-9=0 \\ x^2=9 \\ x=\pm 3 \end{array} \right\} \begin{array}{l} x^2-4=0 \\ x^2=4 \\ x=\pm 2 \end{array}$$

Roots: 3, -3, 2, -2

300 POINTS:

Solve.

$$81x^4 - 1 = 0$$

$$(9x^2-1)(9x^2+1)$$

$$(3x-1)(3x+1)(9x^2+1)$$

$$\left. \begin{array}{l} 3x-1=0 \\ x=1/3 \end{array} \right\} \left. \begin{array}{l} 3x+1=0 \\ x=-1/3 \end{array} \right\} \begin{array}{l} 9x^2+1=0 \\ \frac{9x^2}{9} = -\frac{1}{9} \\ x^2 = -\frac{1}{9} \end{array}$$

Roots: $\frac{1}{3}, -\frac{1}{3}, \frac{i}{3}, -\frac{i}{3}$

$$a = \frac{-1}{9} = \frac{\sqrt{-1}}{\sqrt{9}} = \frac{\pm i}{3}$$

400 POINTS:

Just Factor!

$$8x^6 - 27y^3$$

$$a = 2x^2 \quad b = 3y$$

General form: $(a-b)(a^2+ab+b^2)$

$(2x^2-3y)(4x^4+6x^2y+9y^2)$

500 POINTS:

Just Factor! $2x^4 + 16x$

$$a = x \quad b = 2$$

General form: $(a+b)(a^2-ab+b^2)$

$$2x(x^3+8)$$

$2x(x+2)(x^2-2x+4)$

JEOPARDY**Classifying a Polynomial & Adding/Subtracting Polynomials****100 POINTS:**Write in the following in standard form: $6xy^2 - 8x^3 + 16y^3 - 4x^2y$

$$-8x^3 - 4x^2y + 6xy^2 + 16y^3$$

200 POINTS:Add. $(7r + 2r^4 + 1) + (6r + 3r^4 - 8)$

$$5r^4 + 13r - 7$$

300 POINTS:Subtract. $(6 + 3r + r^2 - 3r^4) - (4 - 2r - 6r^4)$

$$6 + 3r + r^2 - 3r^4 - 4 + 2r + 6r^4$$

$$3r^4 + r^2 + 5r + 2$$

400 POINTS:Simplify. $(8r - 4r^2 + 6r^4) + (2r^3 - r^2 - 7r^4) - (7r^3 - r^4 - 6r^2)$

$$8r - 4r^2 + 6r^4 + 2r^3 - r^2 - 7r^4 - 7r^3 + r^4 + 6r^2$$

$$-5r^3 + r^2 + 8r$$

500 POINTS:

Complete the following table.

Problem	Classify by degree	Classify by term
-10	constant	monomial
$5x^2 - 18$	quadratic	binomial
$7x - 8x^3 + 19 - 12x^2$	cubic	polynomial
$x^4 - 13 + 19x$	quartic	trinomial
$5x - 1$	linear	binomial
$x^4 - 9x^2 - 2x^5$	quintic	trinomial
$x^8 - 10x^2 + 19x - 8x^3 - 5x^9 - x^6$	degree of 9	polynomial

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400 POINTS: Simplify. $(8r - 4r^2 + 6r^4) + (2r^3 - r^2 - 7r^4) - (7r^3 - r^4 - 6r^2)$

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$5x - 1$		
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$x^8 - 10x^2 + 19x - 8x^3 - 5x^9 - x^6$		

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$$8x^6 - 27y^3$$

a =

b =

General form: $(a - b)(a^2 + ab + b^2)$ **500 POINTS:**Just Factor! $2x^4 + 16x$

a =

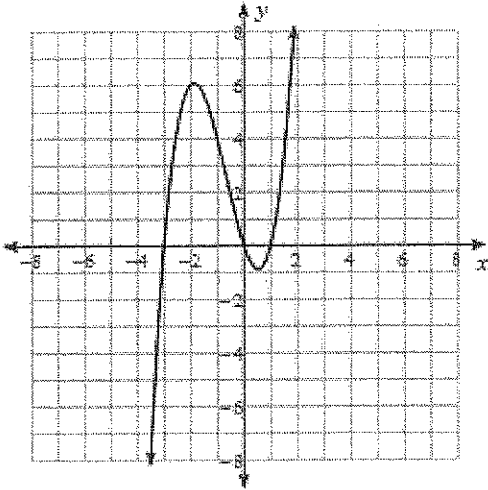
b =

General form: $(a + b)(a^2 - ab + b^2)$

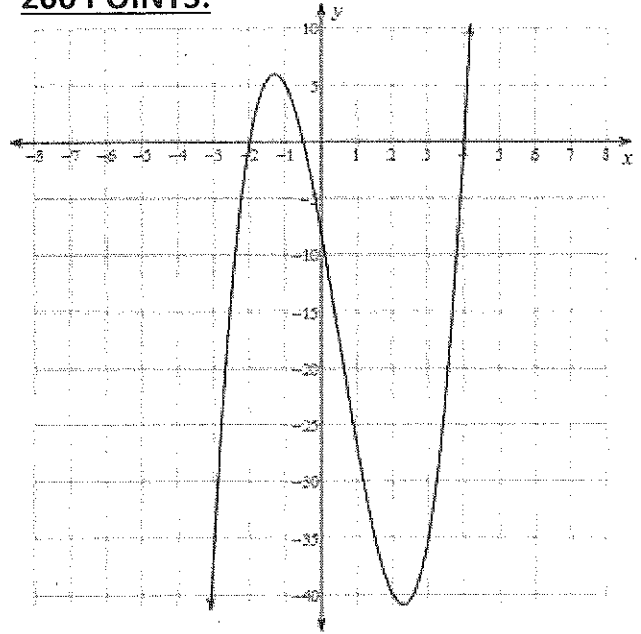
JEOPARDY

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200 POINTS:



300 POINTS:

Write the equation of the polynomial with roots:
 -1 multiplicity 2 and $3i$

400 POINTS:

Write the equation of the polynomial with roots:
 $\frac{-5}{2}$ and $\sqrt{6}$

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